

# 拡散方程式

$$\frac{\partial u}{\partial t} = D \nabla^2 u$$

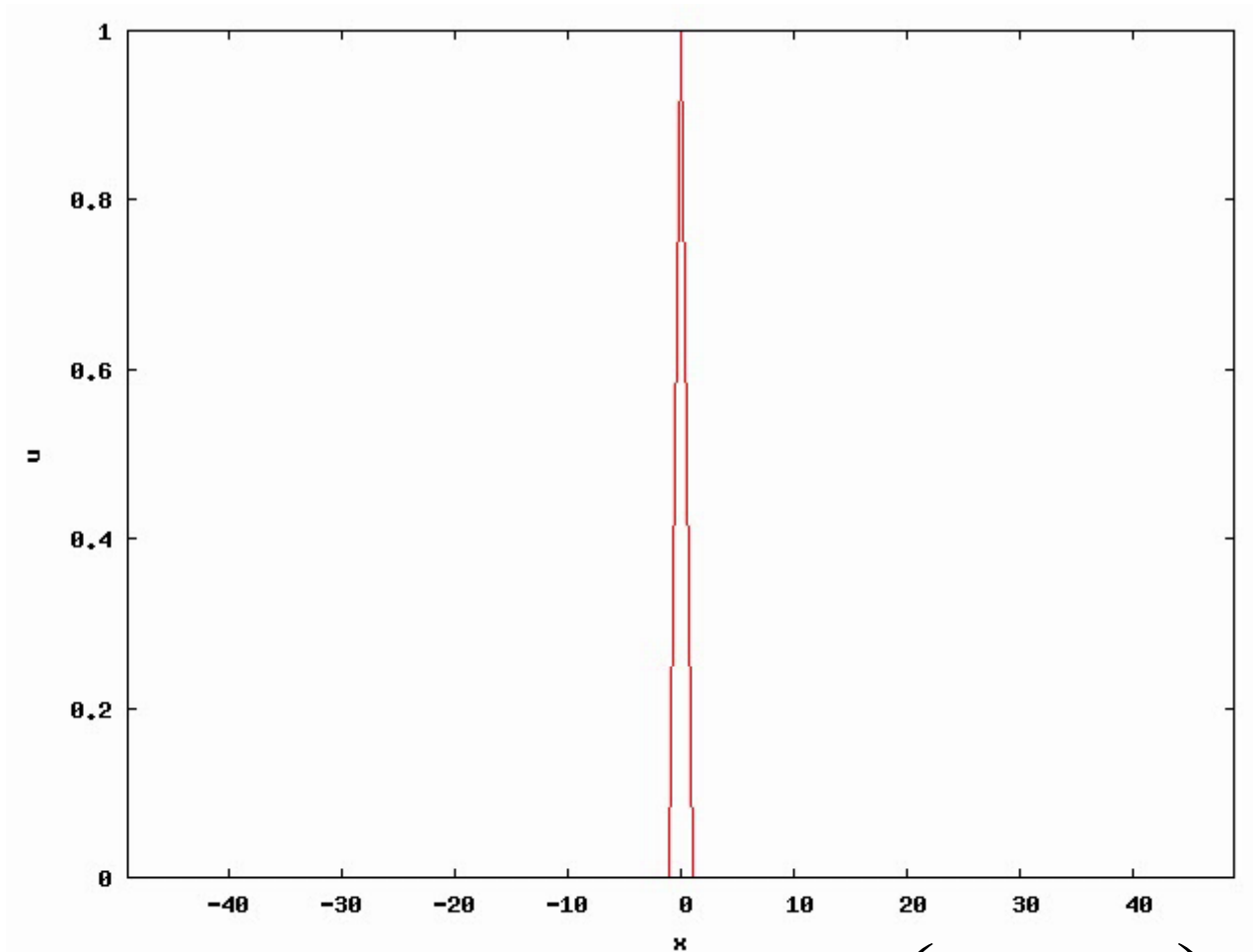
1次元の場合

$$\frac{\partial u}{\partial t} = D \frac{\partial^2 u}{\partial x^2}$$

初期値:

$$u(x, t = 0) = \delta(x)$$

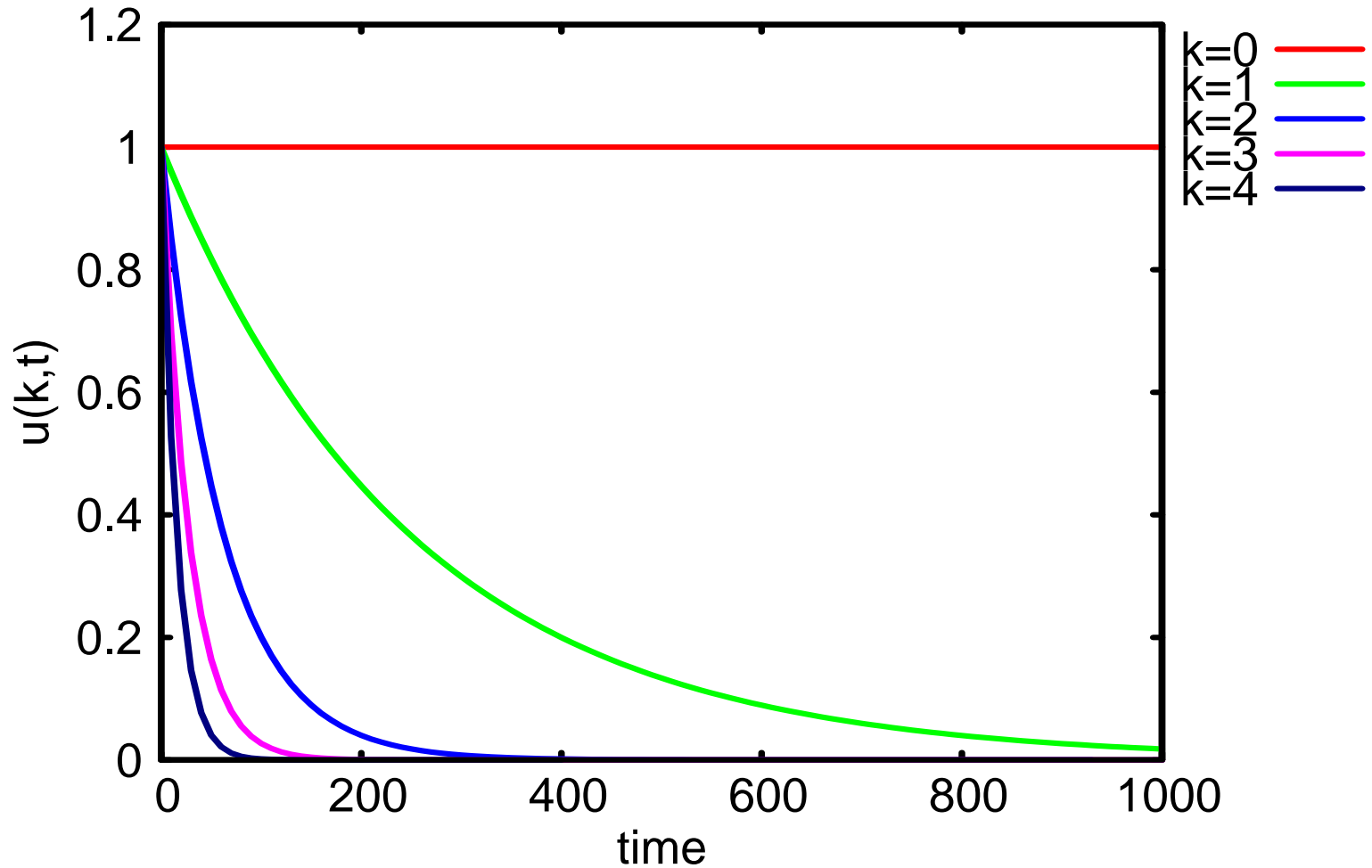
# 1次元で初期値が関数の解 : Green関数



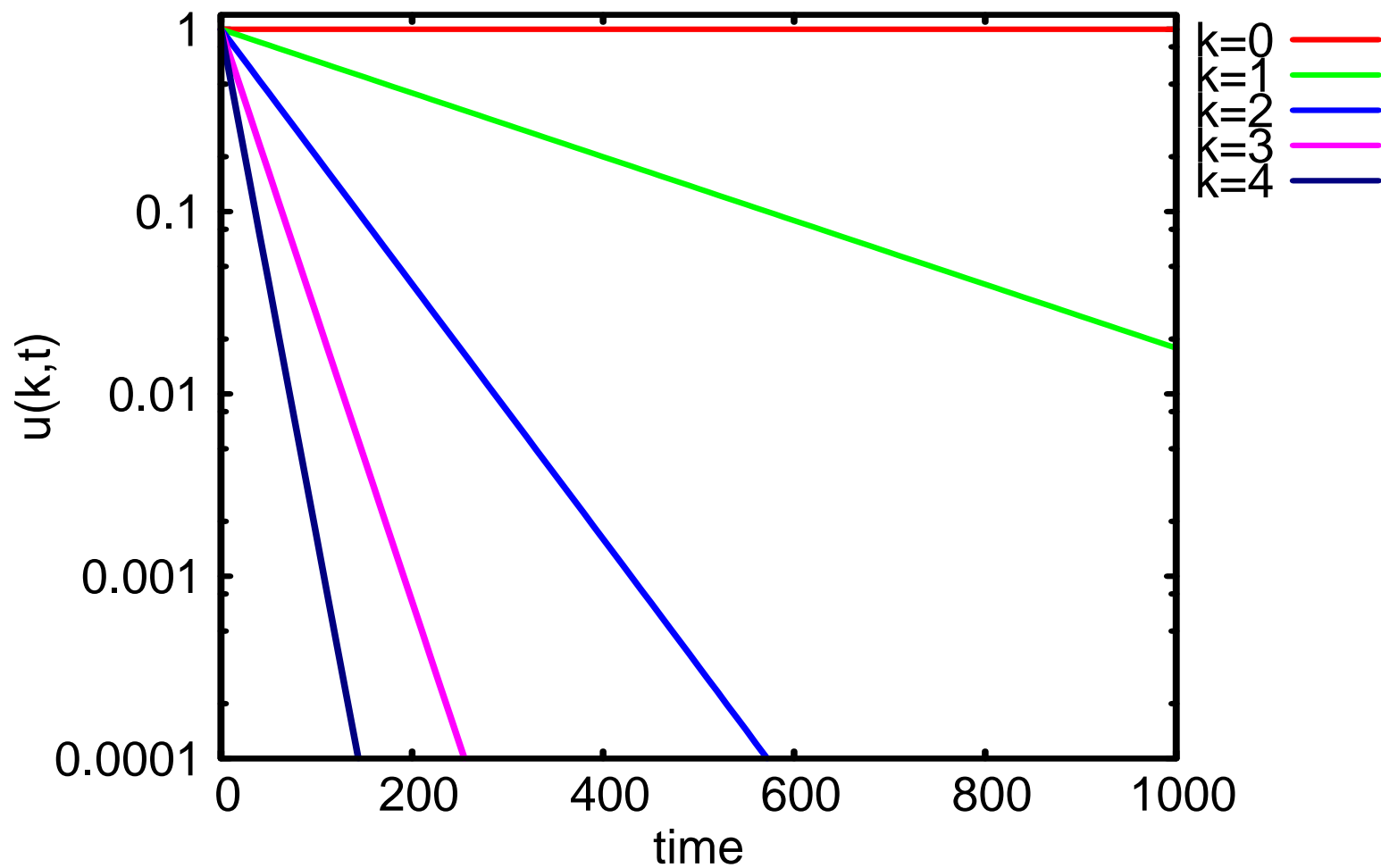
$$u(x, t) = \frac{1}{\sqrt{4\pi Dt}} \exp\left(-\frac{x^2}{4Dt}\right)$$

# Fourier modeの時間変化

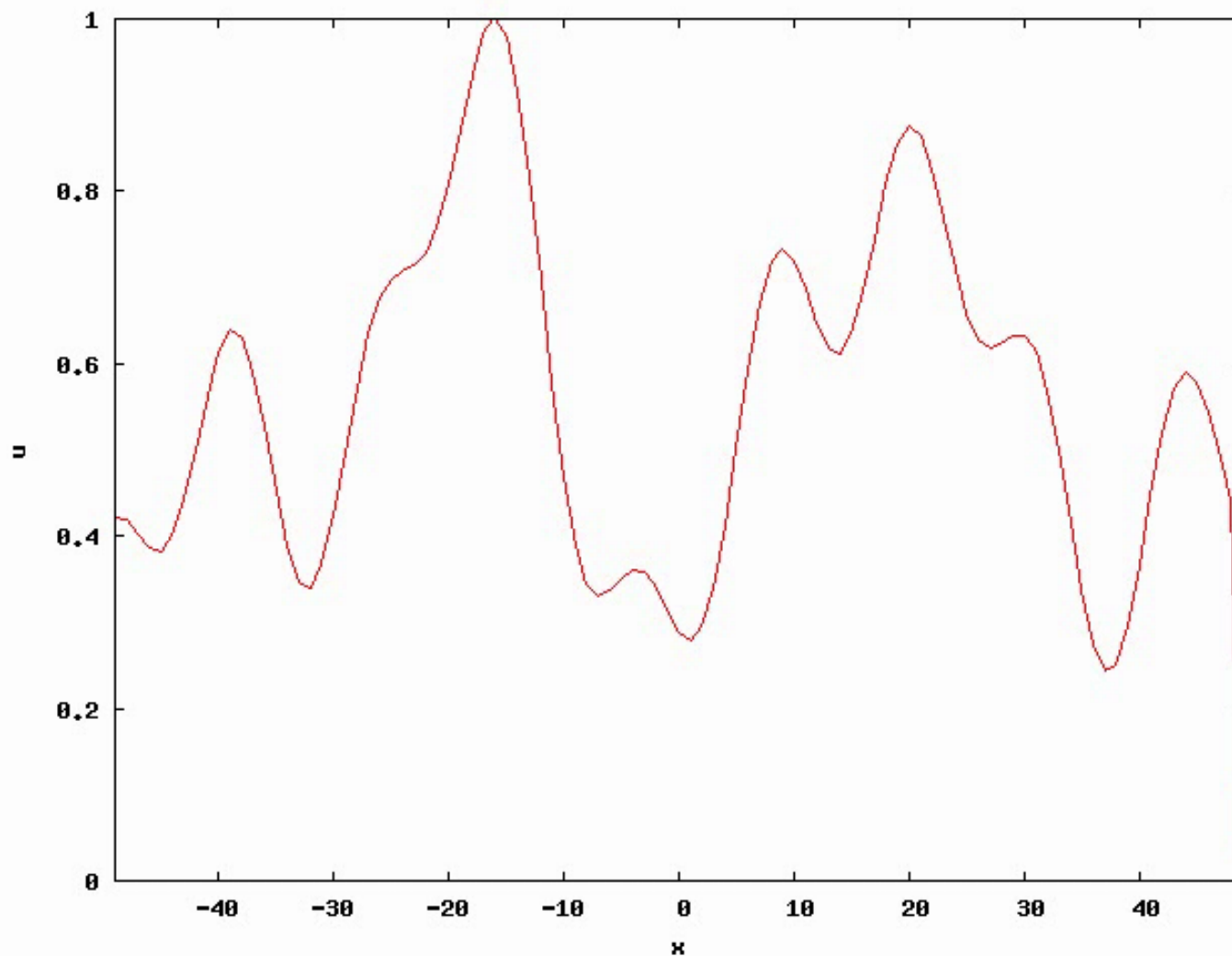
$$u(x,t) = \frac{1}{2\pi} \sum_{k=0}^N \tilde{u}(k,t) \cos\left(\frac{2\pi kx}{NL}\right)$$



Log scaleでは



# 初期値が 関数ではないとき



2次元で初期値が 関数(に近いとき)の解

